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A THEORETICAL INVESTIGATION OF THE STRUCTURE OF EASTERLY WAVES

by

Robert L. Newman



# United States Naval Postgraduate School



## **THESIS**

A THEORETICAL INVESTIGATION OF THE STRUCTURE OF EASTERLY WAVES

bу

Robert L. Newman

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### A THEORETICAL INVESTIGATION OF THE STRUCTURE OF EASTERLY WAVES

by

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#### ABSTRACT

A simple two-level numerical model using the quasi-geostrophic forecast equations is developed. Equations are linearized and friction is introduced in the surface layer. Solutions are obtained numerically by using the initial value approach. Two wind profiles,  $U = -U_0 \tanh y/y_0 \text{ and } U = U_0 \operatorname{sech}^2 y/y_0, \text{ are used and these are known to be unstable. For each wind profile the growth rate is determined as a function of the wave number. Some observed features of easterly waves are reproduced in the numerical solutions.$ 

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#### TABLE OF SYMBOLS AND ABBREVIATIONS

 $A_{e}$  ..... kinematic eddy viscosity

 $\alpha$  ..... inflow angle

 $\theta_0$  ..... derivative of coriolis parameter at y = 0

C ..... specific heat at constant pressure

 $f_0$  .... coriolis parameter at y = 0

g ..... gravity

ω ..... dp/dt

Ψ ..... gz/f

R .... gas constant

ρ ..... density

 $\overline{T}$  .... average temperature from some standard atmosphere

 $\sigma \qquad \dots \qquad (R^2 \overline{T}/p^2 g) (\partial \overline{T}/\partial z + g/C_p)$ 

 $\nabla^2 \Psi$ 

z .... height

#### ACKNOWLEDGMENTS

The author wishes to express his deep gratitude to Dr. Roger Terry Williams for without his patience, guidance, encouragement and counsel this thesis would have been infinitely more difficult.

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#### 1. INTRODUCTION

Synoptic scale disturbances in the tropical atmosphere have long been recognized (Palmer, 1951; Riehl, 1954). In general these disturbances possess a "cold-core" structure with the colder air and most active weather located east of the wave (Yanai and Nitta, 1968b).

Vertical motions associated with these waves are generally upward east of the wave axis and downward to the west (Yanai and Nitta, 1967). The source of energy for these waves is not fully known, however, Charney (1963) argues that when condensation is absent the large scale motions tend to be quasi-horizontal and quasi-nondivergent. If this argument is correct then the barotropic instability that arises as the result of horizontal shear in the Intertropical Convergence Zone could be the source of energy for the disturbances (Schminke, 1968).

Kuo (1949) studied the stability characteristics of a barotropic zonal current, and showed that the barotropic zonal current is stable if the gradient of absolute vorticity has the same sign in the zonal current. Charney (1964) discussed the case where horizontal shear instability is produced in the equatorial convergence zone when the zone is located away from the equator and the converging air masses carry their angular momentum with them.

The purpose of this paper is to devise and test a numerical model that is structured realistically, that is, the perturbation has a configuration and behavior similar to observed easterly waves. The main feature desired is to have the associated weather, and therefore the vertical motion, upwind of the trough axis.

#### 2. BASIS OF THE MODEL

The assumption that the source of energy for the wave mechanism is barotropic instability leads to the selection of a basic current that is independent of height. Baroclinicity has been omitted but the atmosphere remains stratified. Charney (1963) used a scale analysis to show that the barotropic vorticity equation governs tropical motions in the absence of condensation. In another paper Charney (1969) discusses the role of the phase velocity in energy propagation in an easterly regime. Following Schminke (1968) the assumption is made that the easterly waves can be roughly described by a two-level quasi-geostrophic model. It is recognized that the quasi-geostrophic approximation is not very accurate close to the equator, however, the zone of dynamic instability is assumed to be associated with the Intertropical Convergence Zone which is some distance from the equator so that the approximation is relatively accurate.

The type of wind profile chosen will play a large role in determining the stability of the disturbance. Jacobs and Wiin-Nielsen (1966) investigated barotropic instability and found that there are several unstable modes. Since a basic zonal current with no change in the vertical is used in this model, the wave with no vertical motion would predominate (Jacobs and Wiin-Nielsen, 1966). Easterly waves are observed to have vertical motion, so a method must be found to introduce it. This is accomplished by introducing friction in the surface boundary layer. Thus vertical motion, which depends upon the stratification of the atmosphere, is now forced into the model.

#### 3. THE FORECAST EQUATIONS

A simple two-level model is constructed by dividing the entire atmosphere into four layers of constant pressure differential,  $\Delta p/2$  (fig. 1), numbered 0 to 4 from top to bottom. Vertical motion is assumed to be zero at the

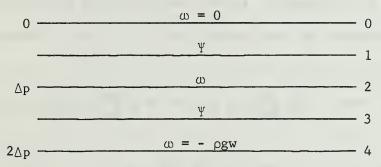


Fig. 1. Two-level model used for prediction.

top of the atmosphere, while the vertical motion term at the earth's surface is

$$\omega \cong - \rho g w_{\underline{\iota}}.$$
 (3.1)

Charney and Eliassen (1949) used the Ekman theory to derive an

expression for  $w_4$  which is  $\frac{1}{2}A_2$ 

$$w_4 = \frac{1}{2} \left( \frac{2A_e}{f} \right) \sin 2\alpha \zeta_4, \qquad (3.2)$$

where  $A_{\mbox{e}}$  is the kinematic eddy viscosity and  $\alpha,$  the inflow angle. The surface geostrophic vorticity can be approximated by

$$\zeta_4 \cong \zeta_3 = \nabla^2 \Psi_3. \tag{3.3}$$

Following the development of Thompson (1961), but using different notation, begin with the quasi-geostrophic vorticity equation

$$\frac{\partial}{\partial t} \nabla^2 \Psi + \left[ k \times \nabla \Psi \cdot \nabla \left( \nabla^2 \Psi \right) + \beta_0 \frac{\partial \Psi}{\partial x} - f_0 \frac{\partial \omega}{\partial p} = 0. \right]$$
 (3.4)

Notice that when  $\omega$  = 0, the above equation becomes the barotropic vorticity equation, which is sufficient to describe the main instability.

Apply this equation at levels 1 and 3 giving

$$\frac{\partial}{\partial t} \nabla^2 \Psi_1 + |k| \times \nabla \Psi_1 \cdot \nabla (\nabla^2 \Psi_1) + \beta_0 \frac{\partial \Psi_1}{\partial x} - f_0 \frac{\omega_2}{\Delta p} = 0, \qquad (3.5)$$

$$\frac{\partial}{\partial t} \nabla^2 \Psi_3 + \left[ k \times \nabla \Psi_3 \cdot \nabla (\nabla^2 \Psi_3) + \beta_0 \frac{\partial \Psi_3}{\partial x} + f_0 \frac{(\omega_4 - \omega_2)}{\Delta p} \right] = 0. \quad (3.6)$$

Smaller layers could be used if it is desired to stop at some intermediate point, say the tropopause, rather than including the entire atmosphere.

Next consider the quasi-geostrophic first law of thermodynamics in the form

$$\frac{\partial}{\partial t} \frac{\partial \Psi}{\partial p} + |k \times \nabla \Psi \cdot \nabla \left( \frac{\partial \Psi}{\partial p} \right) + \frac{\sigma}{f} \omega = 0, \qquad (3.7)$$

where

$$\sigma = \frac{R^2 \overline{T}}{\frac{2}{p}} \left[ \frac{\partial \overline{T}}{\partial z} + \frac{g}{c_p} \right].$$
 (3.7a)

When this equation is applied at level 2 the result is

$$\frac{\partial}{\partial t} (\Psi_1 - \Psi_3) + |k| \times \nabla \frac{(\Psi_1 + \Psi_3)}{2} \cdot \nabla (\Psi_1 - \Psi_3) - \frac{\Delta p \cos_2}{f_2} = 0. \quad (3.8)$$

Define the following quantities

$$\Psi_{\rm m} = \frac{\Psi_1 + \Psi_3}{2} , \qquad (3.9)$$

$$\Psi_{\rm T} = \frac{\Psi_1 - \Psi_3}{2} , \qquad (3.10)$$

which implies that

$$\Psi_1 = \Psi_m + \Psi_T \tag{3.11}$$

$$\Psi_3 = \Psi_m - \Psi_T.$$
 (3.12)

Here  $\Psi_{T}$  is proportional to the layer thickness, therefore is a measure of its mean temperature. Using these definitions add (3.5) and (3.6) and divide the result by 2, obtaining

$$\frac{\partial}{\partial t} \nabla^2 \Psi_{m} + |k \times \nabla \Psi_{m} \cdot \nabla (\nabla^2 \Psi_{m})| + |k \times \nabla \Psi \cdot \nabla (\nabla^2 \Psi_{T})| + \beta_{o} \frac{\partial \Psi_{m}}{\partial x} - f_{o} \frac{\partial \Psi_{d}}{2\Delta p} = 0.$$
(3.13)

For the second forecast equation subtract (3.6) from (3.5) and eliminate  $\omega_2$  using (3.8)

$$\frac{\partial}{\partial t} (\nabla^2 - \mu^2) \Psi_T + |_{k} \times \nabla \Psi_m \cdot \nabla (\nabla^2 - \mu^2) \Psi_T + |_{k} \times \nabla \Psi_T.$$

$$\nabla (\nabla^2 \Psi_m) + \beta_o \frac{\partial \Psi_T}{\partial x} + f_o \frac{\omega_4}{2\Delta p} = 0, \qquad (3.14)$$

where

$$\mu^2 = \frac{2f_0^2}{\Delta p^2 \sigma} . {(3.14a)}$$

These are the prediction equations for the model. They can be linearized by separating the flow into an east-west current that varies only in y, and a small departure from this flow. In this event it is possible to treat various waves in x independently, hence the fields may be defined as follows

$$\Psi_{m} = E(y) + A(y,t) \cos kx + B(y,t) \sin kx,$$
 (3.15)

$$\Psi_{T} = C(y,t) \cos kx + D(y,t) \sin kx, \qquad (3.16)$$

where k is the x wave number.

Substitute expressions for  $\Psi_{m}$  and  $\Psi_{T}$  into (3.13) and (3.14), separate the various sine and cosine terms, neglecting all products of the quantities A through D, and equating coefficients of the cosine kx terms gives

$$\frac{\partial}{\partial t} \left( \frac{\partial^2 A}{\partial y} - A k^2 \right) = k \left[ \frac{\partial E}{\partial y} \frac{\partial^2 B}{\partial y^2} - \frac{\partial E}{\partial y} B k^2 - \frac{\partial^3 E}{\partial y^3} B \right] - \beta_0 B k - K \left( \frac{\partial^2}{\partial y^2} - k^2 \right) (A - C).$$
 (3.17)

For the sine terms the result is

$$\frac{\partial}{\partial t} \left( \frac{\partial^2 B}{\partial y} - Bk^2 \right) = k \left[ \frac{\partial E}{\partial y} Ak^2 - \frac{\partial E}{\partial y} \frac{\partial^2 A}{\partial y^2} + \frac{\partial^3 E}{\partial y^3} A \right] +$$

$$\beta_0 Ak - K \left( \frac{\partial^2}{\partial y^2} - k^2 \right) (B - D).$$
(3.18)

Repeating the procedure for (3.16) the final equations are

$$\frac{\partial}{\partial t} \left( \frac{\partial^2 c}{\partial y^2} - ck^2 - c\mu^2 \right) = k \left[ \frac{\partial E}{\partial y} \frac{\partial^2 D}{\partial y^2} - \frac{\partial E}{\partial y} D \left( k^2 + \mu^2 \right) - \frac{\partial^3 E}{\partial y^3} D \right]$$

$$- \beta_0 Dk + K \left( \frac{\partial^2}{\partial y^2} - k^2 \right) (A - C), \qquad (3.19)$$

and

$$\frac{\partial}{\partial t} \left( \frac{\partial^2 D}{\partial y^2} - Dk^2 - D\mu^2 \right) = k \left[ \frac{\partial E}{\partial y} C \left( k^2 + \mu^2 \right) - \frac{\partial E}{\partial y} \frac{\partial^2 C}{\partial y^2} + \frac{\partial^3 E}{\partial y^3} C \right] + \beta_0 Ck + K \left( \frac{\partial^2}{\partial y^2} - k^2 \right) (B - D),$$
(3.20)

where

$$K = \frac{f_o g}{2RT} \left(\frac{A_m}{f_o}\right). \tag{3.21}$$

It is now necessary to derive the computational equation for vertical motion starting with

$$\omega_2 = \frac{2}{\Delta p \sigma} \left[ \frac{\partial \Psi_T}{\partial t} + u_m \frac{\partial \Psi_T}{\partial x} + v_m \frac{\partial \Psi_T}{\partial y} \right], \qquad (3.22)$$

where

$$u_{m} = -\frac{1}{f_{o}} \frac{\partial \Psi_{m}}{\partial y} , \qquad (3.23)$$

$$v_{\rm m} = \frac{1}{f_{\rm o}} \frac{\partial \Psi_{\rm m}}{\partial x} . \tag{3.24}$$

Substituting equations (3.23), (3.24), (3.15) and (3.16) into (3.22), collecting terms, and again neglecting all products of the quantities A through D results in

$$\omega_{2} = \frac{2}{\Delta p \sigma} \left[ \cos kx \left( \frac{\partial C}{\partial t} - \frac{k}{f_{o}} \frac{\partial E}{\partial y} D \right) + \sin kx \left( \frac{\partial D}{\partial t} + \frac{k}{f_{o}} \frac{\partial E}{\partial y} C \right) \right].$$
 (3.25)

This is the equation used in the model for the computation of vertical motion. The prediction equations and the vertical motion equation are now in the form to be used in the model.

#### 4. BOUNDARY CONDITIONS AND FINITE DIFFERENCING SCHEME

The finite differencing scheme used is illustrated below with a sample variable N;

$$\frac{\partial N}{\partial y} = \frac{1}{2H} \left( N_{i+1} - N_{i-1} \right) \tag{4.1}$$

$$\frac{\partial^{2} N}{\partial y^{2}} = \frac{1}{H^{2}} \left( N_{i+1} - 2N_{i} + N_{i-1} \right)$$
 (4.2)

$$\frac{\partial^{3} N}{\partial y^{3}} = \frac{1}{2H^{3}} \left[ \left( N_{i+2} - 2N_{i+1} + N_{i} \right) - \left( N_{i} - 2N_{i-1} + N_{i-2} \right) \right]$$
(4.3)

where i is the grid index and H is the distance between grid points.

Centered time differences are used for all quantities except those involving friction. The frictional terms are computed at time ( $t - \Delta t$ ). The first step in all cases is a forward time step. The second order equations for time tendencies are solved by the exact method of Richtmyer (1957, p. 101).

Yanai and Nitta (1968a) studied the problem of finite difference approximations in solving dynamic instability problems of non-divergent barotropic currents. They showed that for both symmetric and antisymmetric zonal currents the exact boundary conditions can be replaced by rigid boundary conditions at a distance equal to the half width of the shearing wind belt. At any boundary distance larger than this value the numerical and theoretical values tended to have a constant difference. Therefore rigid boundaries are placed at y = -w/2 and y = w/2, where w is the total width over which computations are made. With the exception of E (the basic current) all variables have the boundary condition A = B = C = D = 0 at y = -w/2 and at y = w/2. When second derivatives are required on the boundary they are set equal to zero.

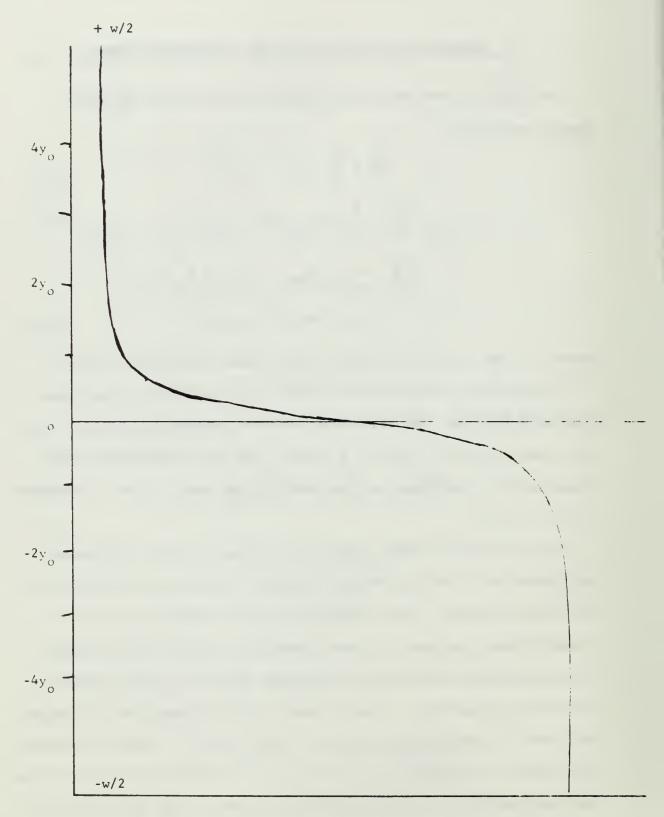


Fig. 2. Wind profile  $U = -U_0 \tanh y/y_0$ .

#### 5. WIND PROFILES AND INITIAL CONDITIONS

Schminke (1968) investigated and discussed the structure of easterly waves from a similar model using one wind profile  $(U = -U_0 \tanh(y/y_0))$  and one non-dimensional wave number  $(1/2y_0)$ . It is proposed to expand this to include another profile  $(U = U_0 \operatorname{sech}^2 y/y_0)$ . Additionally the behavior of disturbances at various non-dimensional wave numbers under both profiles will be considered.

Charney (1963) shows by scale analysis that in the absence of condensation, flow in the tropics is governed by the barotropic vorticity equation. The assumption is made that the source of energy for easterly waves must be barotropic instability. Since potential energy is assumed not to be an important energy source the basic temperature field may be set equal to a constant and is invariant. However, small temperature fluctuations are observed with easterly waves, so a two level model is needed (Schminke, 1968).

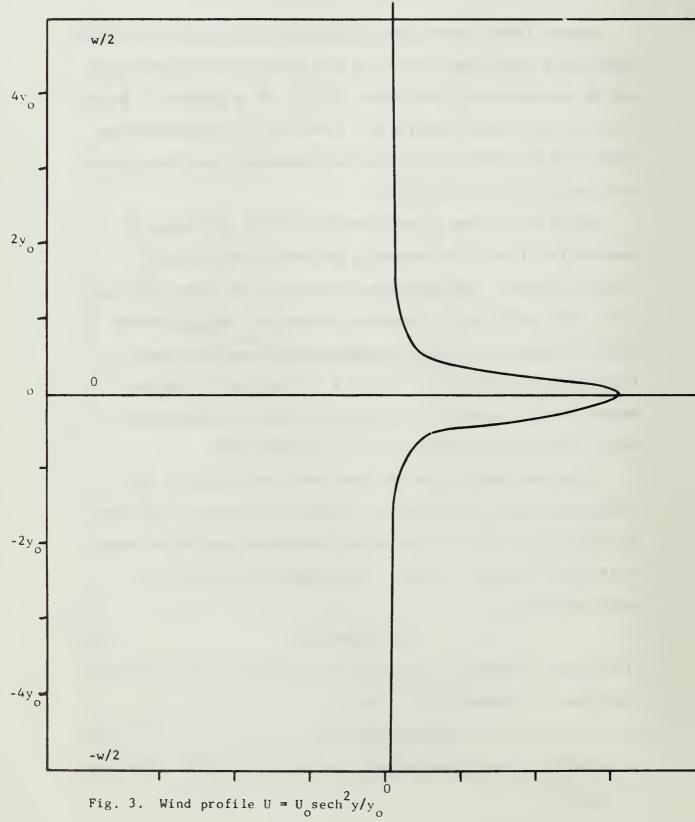
If the waves are to grow, the zonal wind profile must be baro-tropically unstable. Following the suggestion of Charney (1963) that the shear layer near the Intertropical Convergence Zone may be formed by transport of angular momentum, the unstable profile chosen to approximate this is

$$U = -U_0 \tanh y/y_0, \qquad (5.1)$$

illustrated in figure 2. This seems most appropriate during monsoonal conditions. The second profile chosen,

$$U = U_0 \operatorname{sech}^2 y/y_0 , \qquad (5.2)$$

is probably more applicable to mean flow conditions, and is illustrated in figure 3.



Garcia (1956) found that the profile given in (5.1) is barotropically unstable when  $0 \le k \le y_0^{-1}$ . Betchov and Criminale (1967) have analytically, and by use of the eigenvalue approach, investigated this profile throughout the range mentioned above and found the maximum instability at a non-dimensional wave number of 0.45 (ky\_0 = 0.45). With these results in mind this paper is confined to the range 0.25 to 0.60 for the non-dimensional wave number when dealing with the hyperbolic tangent profile (5.1). Betchov and Criminale (1967) found a rather flat zone of maximum instability for the hyperbolic secant squared profile (5.2) in the range 0.80 to 1.05 for the non-dimensional wave number. Some computations were done in the lower range (0.25 to 0.60), but the majority of the experiments with this profile were confined to the range 0.70 to 1.15. Results of experiments with both profiles will be discussed in a later section.

With the wind profile independent of height and with no friction  $\Psi_{\mathbf{m}}$  and  $\Psi_{\mathbf{T}}$  should behave independently. Jacobs and Wiin-Nielsen (1966) showed that the growth rate for the  $\Psi_{\mathbf{m}}$  field is greater than that for the  $\Psi_{\mathbf{T}}$  field. The thermal field  $\Psi_{\mathbf{T}}$  is zero in the initial state but it changes as a result of the Ekman friction term.  $\Psi_{\mathbf{m}}$  is introduced into the model as a random disturbance in y. Introduction of surface friction leads to the coupling of the two fields. Thus at time t = 0

$$A = random disturbance (y),$$
 (5.3)

$$B = random \ disturbance \ (y),$$
 (5.4)

$$C = 0 \tag{5.5}$$

$$D = 0$$
 (5.6)

$$E = U_0 y_0 \ln(\cosh(y/y_0)), \qquad (5.7)$$

$$E = U_{o} y_{o} \tanh y/y_{o}. \tag{5.8}$$

or

#### 6. COMPUTATIONAL PROCEDURE

A list of the constants used in the computations is given below;

y = 200 kilometers,

w = 2000 or 4000 kilometers,

 $U_{o} = 10$  meters per second,

 $f_0 = 5 \times 10^{-5}$  per second,

 $\sigma = 0.8$  meters per second squared per centibar squared,

 $\beta$  = 0.0 or 2.29 x 10<sup>-11</sup> per meter per second,

 $\Delta p = 50$  centibars,

 $A_0 = 10$  meters per second squared,

 $\alpha = 22.5 \text{ degrees},$ 

 $\mu^2 = 2.49 \times 10^{-12}$  per meter squared,

H = 25 or 50 kilometers,

 $\Delta t = 0.5$  or 1.0 hours.

When w = 2000 km and H = 50 km a forecast period of 14 days was used, in all other cases the forecast period was 28 days. A sample program as developed by Schminke (1968) and modified to fit the IBM 360 computer is included as Appendix 1 (note: this program is for w = 2000 km and H = 25 km).

The random disturbance introduced into the  $\Psi_{m}$  field, (5.3) and (5.4), was generated by a random number generation program, then read directly into the computer. The same disturbance field was used for all experiments with both variations of  $\beta$ , H,  $\Delta t$ , and all variations of the non-dimensional wave number. After a few days the disturbance adjusted to an exponential growth. For convenience, growth rates were computed over the last three days of the forecast period. Once the field has adjusted it does not matter when computed, rates are always

the same. This was done by assuming the amplitudes could be written as

$$x_1 = Sexp (U_o n/y_o) t_1,$$
 (6.1)

$$x_2 = Sexp (U_o n/y_o) t_2,$$
 (6.2)

where n is the growth rate and S is a constant. By forming the ratio  $x_2/x_1$ , the growth rate can be shown to be

$$n = \frac{y_0 \ln (x_2/x_1)}{U_0 (t_2 - t_1)}. \tag{6.3}$$

#### 7. RESULTS

A series of experiments was conducted under varied conditions. In general the total distance over the grid was 2000 km, but one series was done over a total distance of 4000 km. Grid mesh was either 50 km or 25 km with the smaller distance producing better results. When the grid mesh was 25 km a time step of 0.5 hours was used, however the majority of experiments were run at t = 1.0 hours. All cases were run with  $\beta$  = 0, then with  $\beta$  = 2.29 x 10  $^{-11}$  meters per second. Many combinations of friction, wave number and wind profile were run, and selected ones are illustrated in figures 4 through 19.

Growth rates for the disturbances with both profiles and for various non-dimensional wave numbers are shown in figures 4 through 11. Betchov and Criminale (1967) found a maximum growth rate of approximately 0.19 for a non-dimensional wave number of 0.45 using the hyperbolic tangent profile. With rigid boundaries, no friction and a fairly large grid size (H = 25 km) through the maximum shear zone (width approximately 400 km), the result (fig. 7) was a growth rate of 0.165 at a wave number of 0.45. According to Yanai and Nitta (1968a) the best results should be obtained with a minimum of 20 grid steps across the zone of maximum shear. Therefore the results for the hyperbolic tangent profile are considered good, and the trend upward toward the Betchov and Criminale (1967) results is evident as the grid size is decreased (compare figures 5 and 7). The inclusion of the 8 parameter had no significant effect on the growth rates giving only a slight decrease of 0.01 or less.

The hyperbolic secant squared profile results were equally encouraging. Just as Betchov and Criminale (1967) lead one to expect, a relatively broad zone of maximum growth is found reaching from 0.85 to 0.95 non-dimensional wave numbers. It is difficult to ascertain just what maximum rate Betchov and Criminale (1967) found, however, results of these experiments show rates that are significantly smaller than the rates for the hyperbolic tangent profile. The inevitable conclusion is that the hyperbolic secant squared profile is not quite as unstable as the hyperbolic tangent profile. As before, decreasing the grid size in the maximum shear area led to larger growth rates. Figures 9 and 10 illustrate this very well.

In figures 12 through 15 the amplitude and phase relationships of  $\Psi_m$ ,  $\Psi_T$  and  $\omega$  are depicted for the wave number of maximum growth. Amplitudes of  $\Psi_m$ ,  $\Psi_T$  and  $\omega$  show maxima in the region of greatest horizontal shear. The influence of the frictional term is clearly seen in the relative amplitudes of  $\Psi_1$  and  $\Psi_3$ . The three fields show close phase relationships and all phases change rapidly through the shear zone. It appears to be a safe assumption that the temperature and pressure fields are in close relation for both levels. The omega amplitude (fig. 14) shows a distinct minimum in the center of the field but sharp maximum peaks on each side in the maximum shear zone. Phase relations between  $\Psi_3$  and  $\omega$  might almost be termed ideal with the sinking motion north of the shear zone about 70 degrees upwind of the amplitude ridge, placing the convergence in the area where it is normally observed in easterly waves.

Addition of the  $\beta$  parameter made small insignificant changes in the amplitude; phase relationships maintained the same basic pattern as

without  $\beta$ . Variation in the non-dimensional wave number over the range 0.25 to 0.60 left the pattern basically unchanged while producing the growth rate changes discussed above.

Figures 16 through 19 illustrate the behavior of the hyperbolic secant squared profile. Note that  $\Psi_1$  far exceeds the other components in amplitude (fig. 16) and that the maximum is symmetrical around the center of the maximum shear zone.  $\Psi_3$  is very small indicating that friction is probably more effective with the hyperbolic secant squared profile. The lower field,  $\Psi_3$ , tends to lead the upper field in westward movement. This appears reasonable and is observed in tropical disturbances of this nature (Riehl, 1954, pp. 215). This gives the entire system a tilt toward the east with increasing height; this tilt is not noticeable with the hyperbolic tangent profile.

The omega amplitude is very sharp peaked and symmetric about the center. Velocities, from about  $\pm$  y<sub>o</sub> to the boundaries, are very small. In this area the convergence appears to be about 100 degrees out of phase with the trough. Near y<sub>o</sub> = 0, along the Intertropical Convergence Zone, the convergence actually leads the trough.

Use of a finite value for the  $\beta$  parameter made no significant difference in the results with this profile.

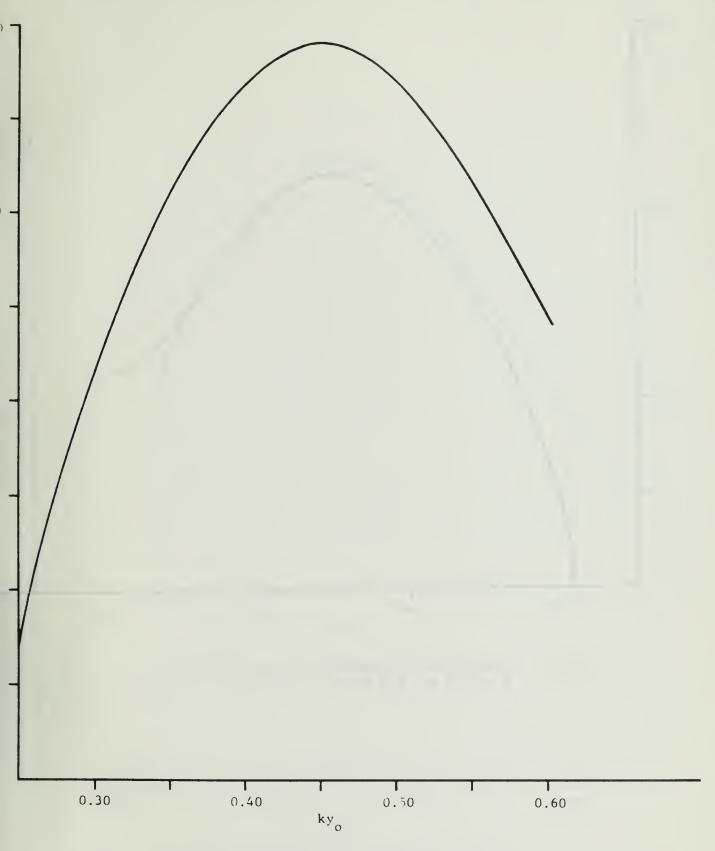


Fig. 4. Growth rate for hyperbolic tangent profile, w = 2000 km, H = 50 km, with friction.

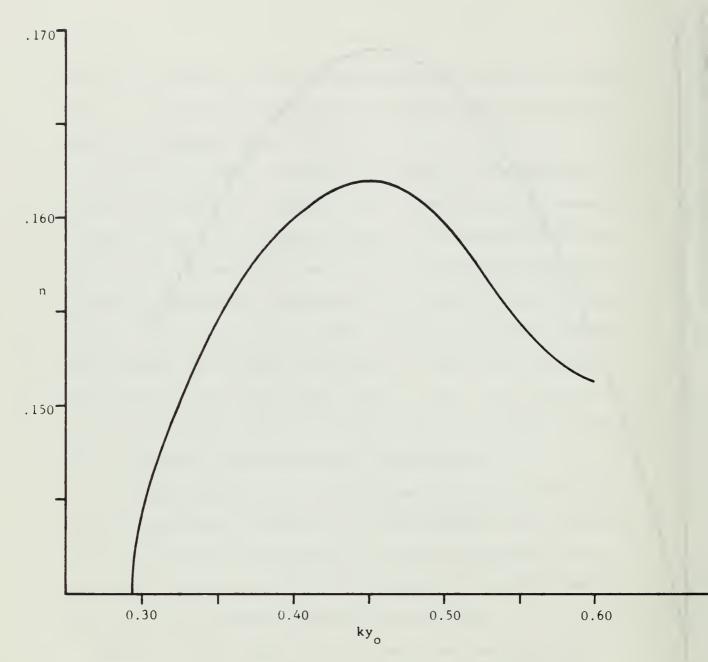


Fig. 5. Growth rate for hyperbolic tangent profile, w = 2000 km, H = 50 km, no friction.

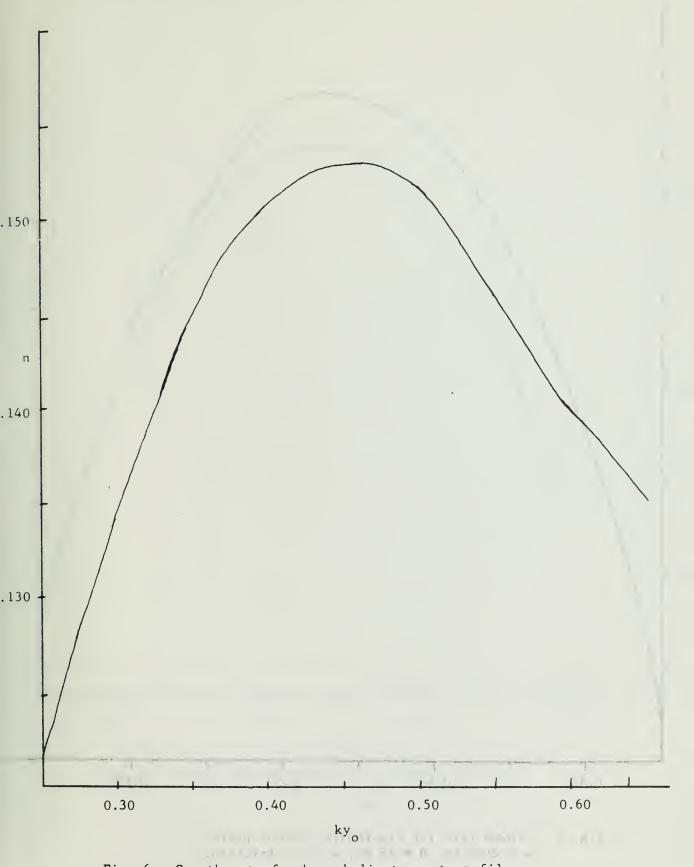


Fig. 6. Growth rate for hyperbolic tangent profile, w = 2000 km, H = 25 km, with friction

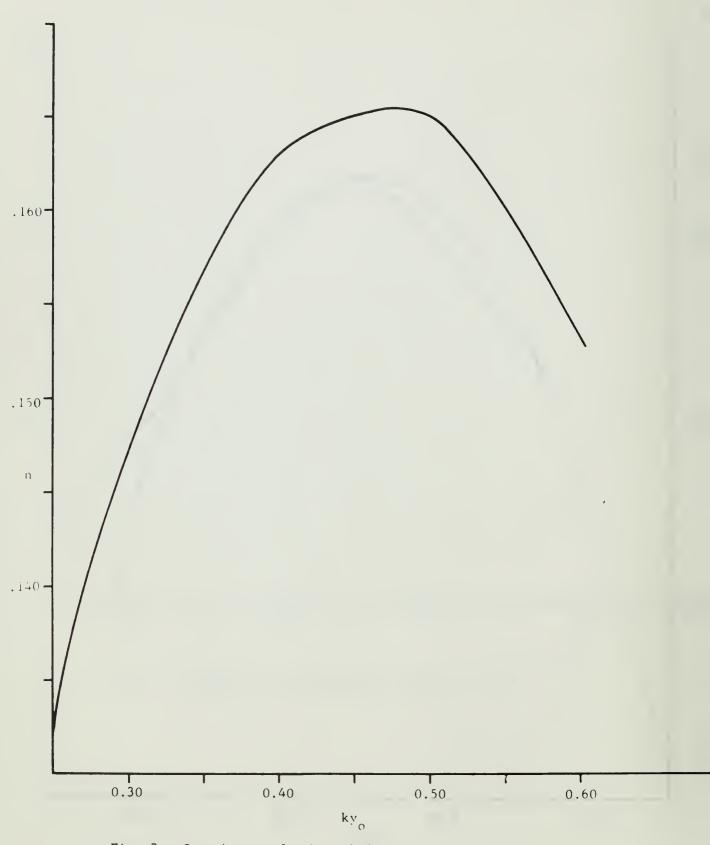


Fig. 7. Growth rate for hyperbolic tangent profile, w = 2000 km, H = 25 km, with no friction.

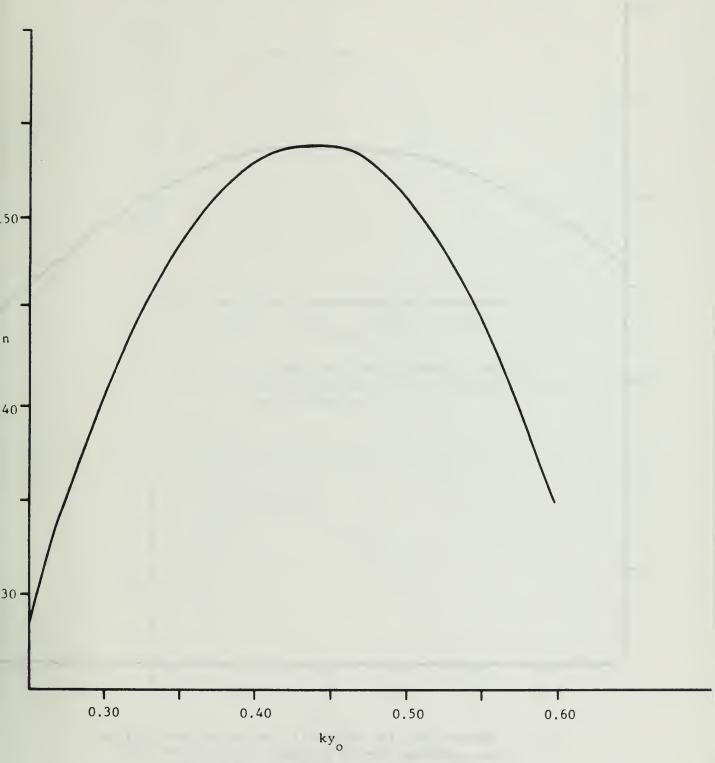


Fig. 8. Growth rate for hyperbolic tangent profile, w = 4000 km, H = 50 km, with friction.

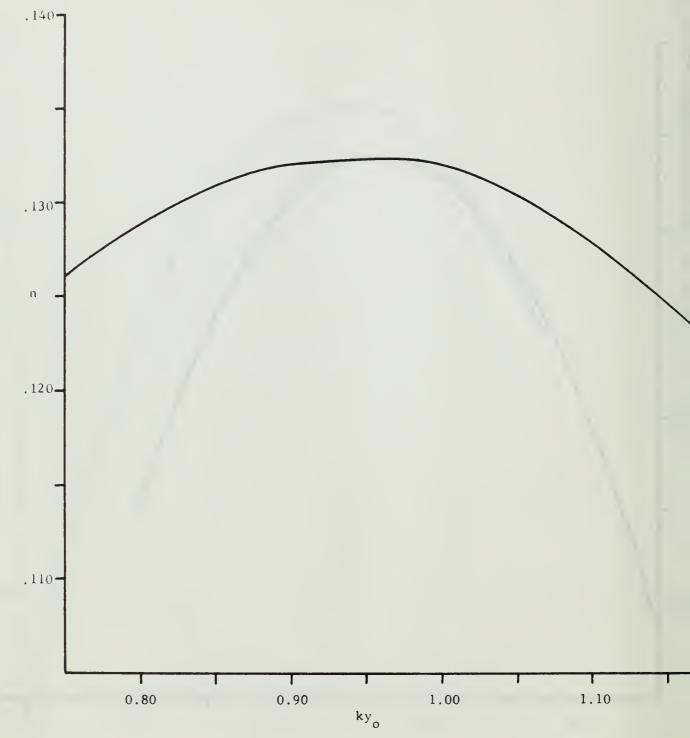


Fig. 9. Growth rate for hyperbolic secant squared profile, w = 2000 km, H = 50 km, with friction.

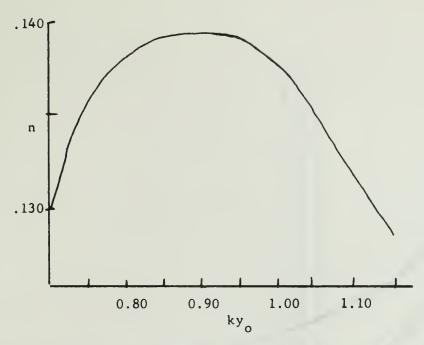


Fig. 10. Growth rate for hyperbolic secant squared profile, w = 2000 km, H = 25 km, with friction.

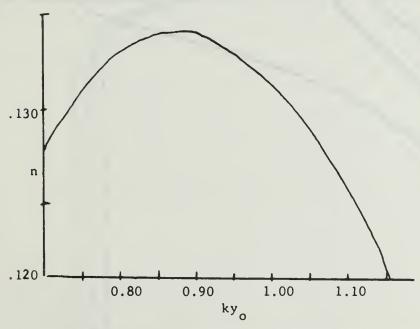


Fig. 11. Growth rate for hyperbolic secant squared profile, w = 4000 km, H = 25 km, with friction.

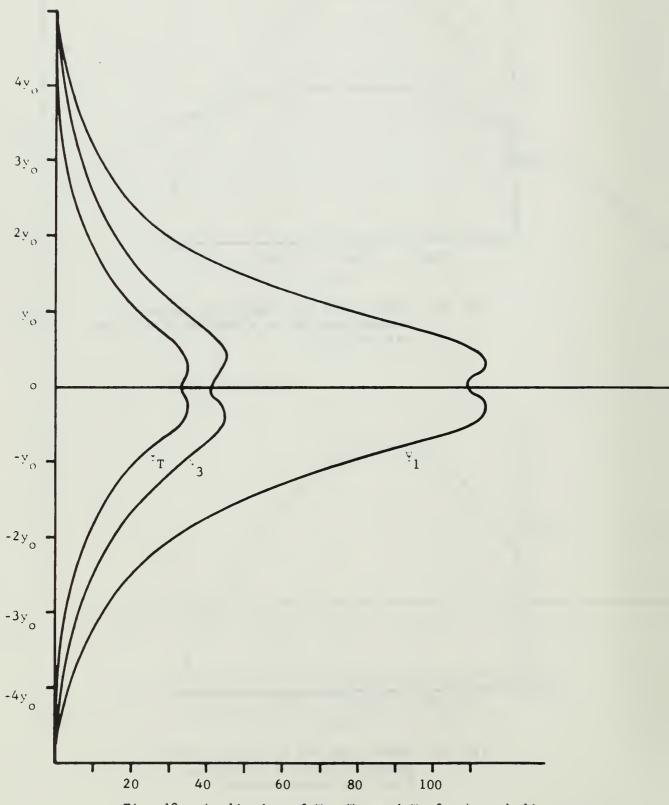


Fig. 12. Amplitudes of  $\Psi_T$ ,  $\Psi_1$ , and  $\Psi_3$  for hyperbolic tangent profile plotted against arbitrary scale, w = 4000 km, H = 50 km, and wave number = 0.45.

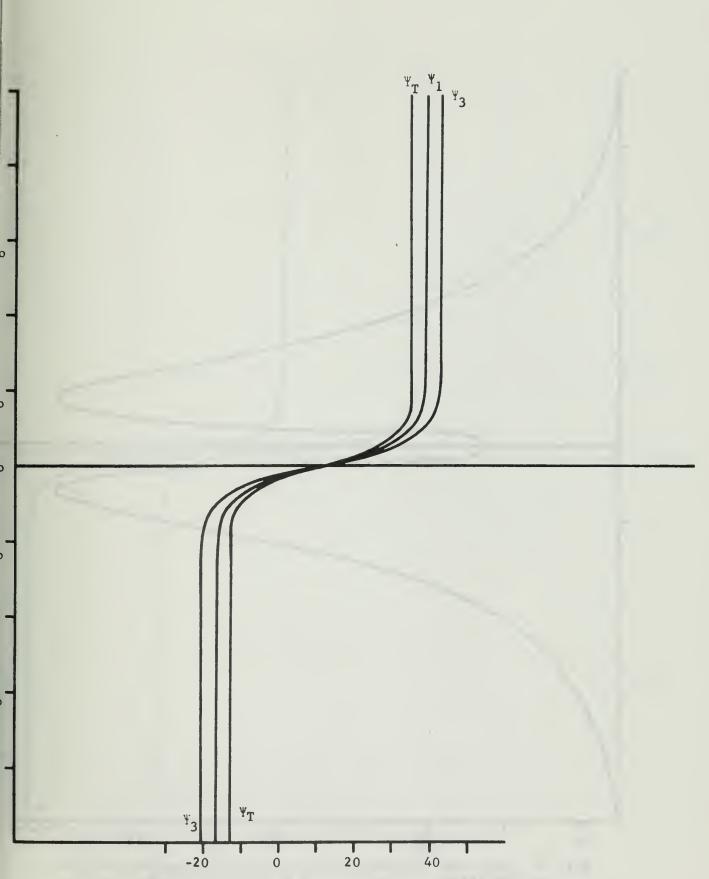


Fig. 13. Phase relationships corresponding to amplitudes of fig. 12.

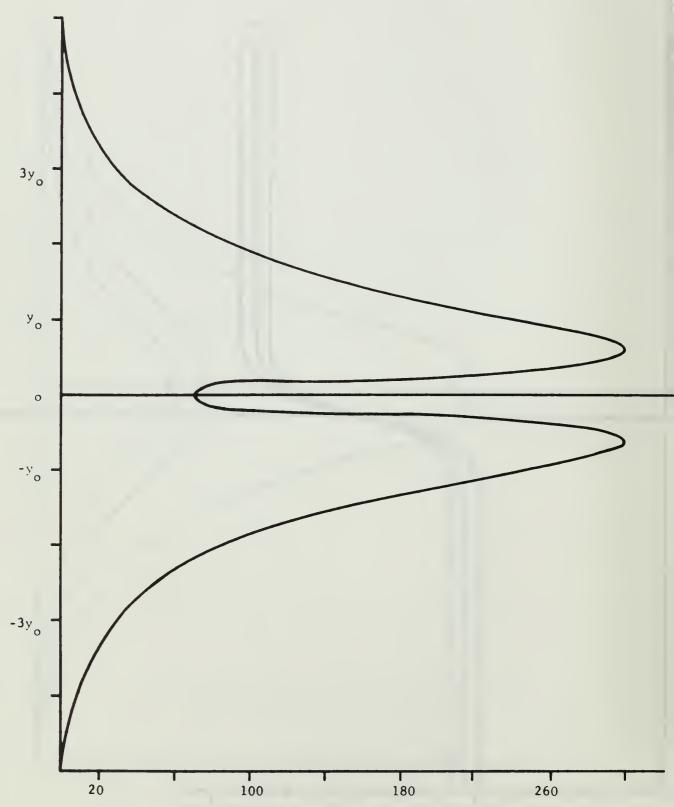


Fig. 14. Amplitude of omega, arbitrary scale for same case as figs. 12 and 13.

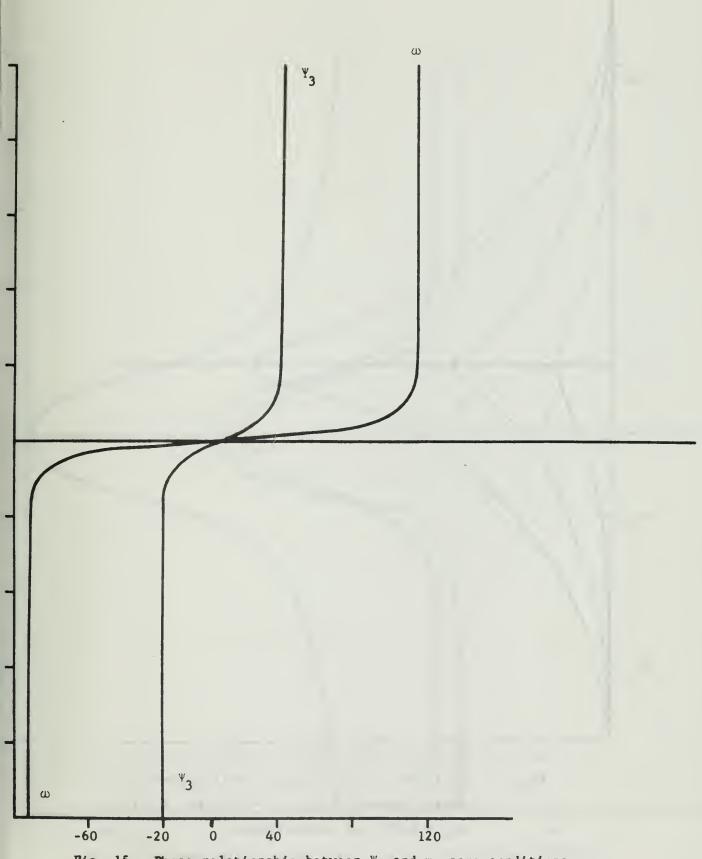


Fig. 15. Phase relationship between  $\Psi_3$  and  $\omega$ , same conditions as figs. 12, 13, and 14.

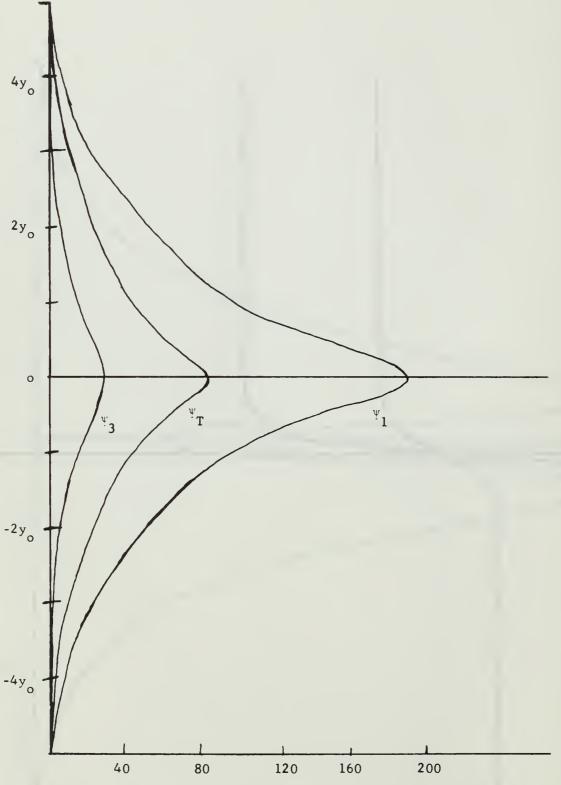


Fig. 16. Amplitude of  $\Psi_1$ ,  $\Psi_3$ , and  $\Psi_T$  with hyperbolic secant squared profile, w = 2000 km, H = 25 km,  $ky_0$  = 0.95, and scale arbitrary.

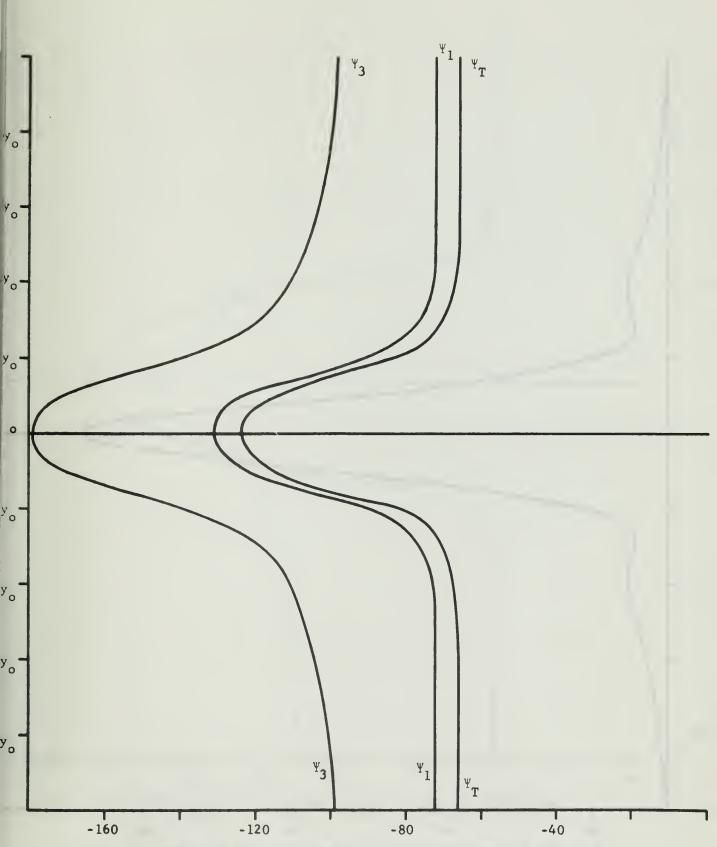


Fig. 17. Phase relationship for  $\Psi_1$ ,  $\Psi_3$ ,  $\Psi_T$  for same conditions as fig. 16.

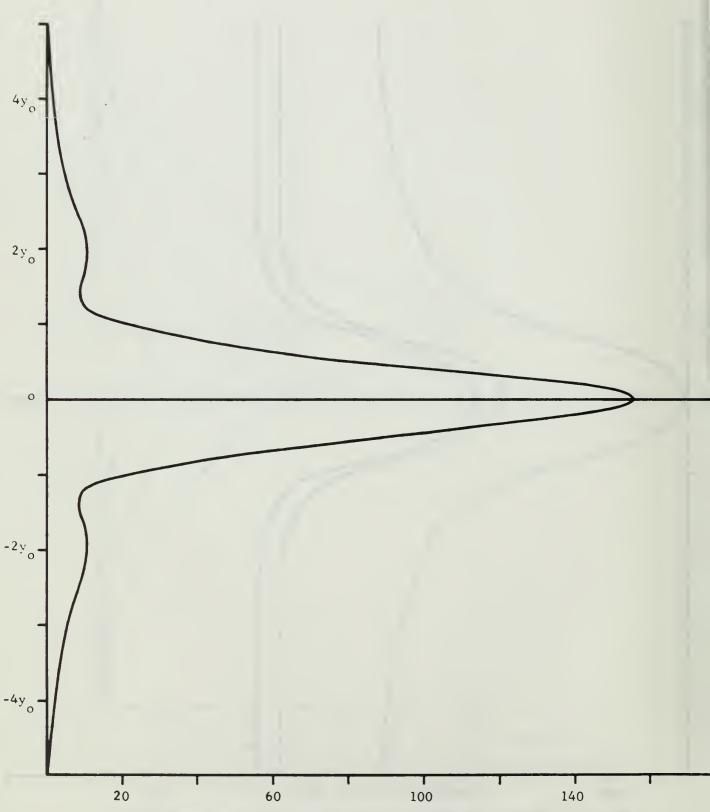


Fig. 18. Amplitude of omega, conditions as in fig. 16.

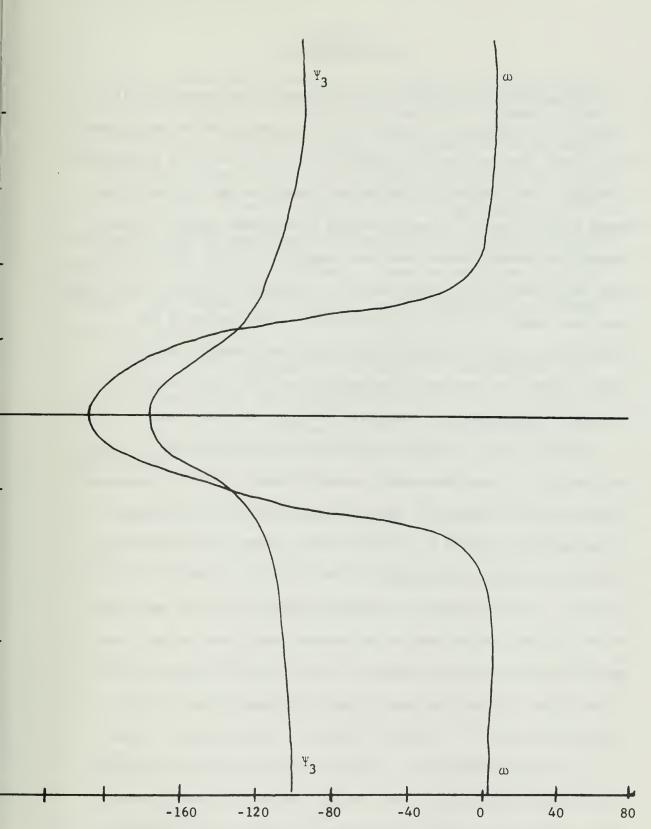


Fig. 19. Phase relationship between omega and  $\Psi_3$  for conditions in fig. 16.

## 8. CONCLUSIONS

The easterly wave model developed appears to be reasonable if the assumption of barotropic instability as the energy source is accepted. Basic zonal flow has been introduced by two profiles, both independent of height. The temperature variations arose from the action of the Ekman friction terms. Waves developed by the model behaved in many respects as easterly waves have been observed to act. Results show that the growth rate of disturbances is a function of wave number, therefore wave length, as well as other factors. Separation of the boundaries to greater distances made some small changes but the greater effect is obtained by decreasing the grid size, which also required changing the time step size, through the shear zone.

Vertical motions produced by the hyperbolic tangent profile are very similar to those observed in easterly waves, in that the maximum sinking motion is upwind of the lower level ridge and the maximum rising motion is upwind of the lower level trough. The disturbance maintains its phase relationship in the vertical so that no tilt is observed. With the hyperbolic secant squared profile the amplitude of the vertical motion outside the maximum shear zone is small and again the rising motion is upwind of the trough and sinking upwind of the ridge. Within the area of large horizontal shear the convergent area moves to a position downwind of the low level trough. It is not known whether this is observationally verified along the Intertropical Convergence Zone. Using this profile, the hyperbolic secant squared, the model has developed a solution that indicates a definite eastward tilt with height. This tilt has been verified by observations. Perhaps some combination of the two profiles would be more realistic in depicting actual waves.

A more complete investigation of the effect of friction on the symmetric secant squared profile appears warranted. There is, also, a definite need to include the effects of condensation in the model.

Non-linear effects, their role in changing the mean wind profile and the structure of the disturbance, are very important and must be considered. Use of the primitive equations or the balance equations would seem to offer the most effective means of incorporating these effects. They appear to be crucial if an easterly wave is to grow into a tropical storm.

Always of utmost importance is the need for more detailed and extensive observations, but nowhere is this as true as of the tropics.

No model can be developed and adequately tested without detailed observations.

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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               PAST ARRAY AND THE FUTURE DATA INTO THE PRESENT ARRAY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FIRST TIME INTEGRATION
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    MAIN LOOP FOR FORECASTING
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               F(NCOUNT.LT.336) GO TO 800
                                                                                                                                                                                                                                                                                                                                                                                                      I=1,N
                                                                                                                              THE CONTROL OF THE CO
ATDF(I)
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     FORMAT(1H , I3, 28, 3X, I3)
DO 930 I = 1, N
IK = N-I+1
WRITE(6, 932) I
WRITE(6, 932) I
                                                                                                                                                                                                                                                                                                                TTOOR
                                                                                                                                                                          00
                                                                                                                                                                                                                                  IF ( TEST2 .LT. 2.0 )
                                                                                                                                                                                                                                                                     NXT = NXT + 1
NXTPRT = NXTPRT+ 1
                                                                                                                                                                                                                                                                                                         CONTINUE
                                                                                                                                             COMPUTE THE HEADINGS
                                                                                                                                                           PRINT OUT OF DATA
                                                                                                                                                                                                     IF (NXT .LT. NRUN) GO TO
                                                                                                                                                                                                                    TEST FOR END OF RUN
                                                                                                                                                                                                                                                        TEST FOR PRINTOUT
                                                                                                                                                                                                                                                                                          INCREMENT COUNTERS
                                                                                                                                                                                       HAVE REACHED THE MAX NUMBER
                                                                                                                                                                          TO 901
                                                                                                                                                                                                                                                                                                                 . . . . . . . . .
                                         I3,3X,E16.8,3X,E16.8,3X,E16.8
     IK, ATDPR(N-I+1), BTDPR(N-I+1), CTDPR(N-I+1), ETDPR(N-I+1), FTDPR(N-I+1), IX
                                                                                                           HOR
                                                                   INTEGRATION NUMBER, 14, 25H, INTEGRATION NUMBER, 14, 25H,
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000 000 0 000 FAKE = 0.1E-19
DO 220 I =1.N
I J = 1.1
I J GO TO 292
IF( I .EQ. 1) GO TO 292
ESY(I) IS CALCULATED IN ENERGY AND DOES NOT HAVE TO BE REPEATED.
WC (FSY(N-I+1) \* BTDPR(N-I+1)-CTDPA(N-I+1))/(2.0\*TIME) + FUK
2\*((FSY(N-I+1) \* BTDPR(N-I+1)-CDY(N-I+1) \* DTDPR(N-I+1)) )
4CTDPR(N-I+1) \* UCONST \* ((DTDF(N-I+1)-DTDPA(N-I+1))/(2.0 \* TIME) +
4CTDPR(N-I+1))
WS
FUK\*((ESY(N-I+1)))
FUK\*((ESY(N-I+1)) CTDPR(N-I+1)-DTDPA(N-I+1))/(2.0 \* TIME) +
2FUK\*((ESY(N-I+1)))
FUK\*((S/SOMU)\*((BDY(N-I+1)-DDY(N-I+1)) \* ATDPR(N-I+1))
FUK\*((ABS(UM)\*(I-I+1)) -FSY(N-I+1)) -SQK\*(BTDPA(N-I+1)4CTDPA(N-I+1))
FUK\*((ABS(UM)\*(I-I+1)) -FSY(N-I+1)) -SQK\*(BTDPA(N-I+1))
FUK\*((ABS(UM)\*(I-I+1)) -SQK\*(BTDPA(N-I+1)) -SQK\*(BTDPA(N-I+1 298 297 299 222 CALL ENERGY
FECNT = FECNT + 1.0
FEPRT IS RELATIVE TO THE N
IF (FECNT LT. FEPRT ) GO 1
WRITE(6,222)
2 FORMAT(1HO,115H I AMPLITU
2 FORMAT(1HO,115H PHASE2,C,0 ZTRPPPPPCCWAMANA AMAMANA AMAMA NON COMPUTE AKE S **ALCULATE** PHASE USED 10 THE ANGLE I AMPLITUDE PHASE2,C,D PREVENT ENERGY Z DEGREES DIVISION NUMBER TO 911 RELATIONSHIPS OF. 유 D 8¥ AND B TIMES ZERO QF 2 PRINTOUT THE PHASE, A I **BOUNDAR I E** OCCURS PHASE3, WC, WS ) FUX.

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NASSUT 293
IT CONTINUE ATAN(BTDPR(N-I+1)/ATDPR(N-I+1))
PHASE ATAN(BTDPR(N-I+1)/ATDPR(N-I+1))
RO CAMPI = ATDPR(N-I+1)/COS(PHASE)
GO TO 95
90 CAMPI = BTDPR(N-I+1)/SIN(PHASE)
90 CAMPI = BTDPR(N-I+1)/SIN(PHASE)
90 CAMPI = BTDPR(N-I+1)/SIN(PHASE)
91 F ( CAMPI - GE. 0.0) GO TO 119
1F ( CAMPI - GE. 0.0) GO TO 115
112 PHASE = PHASE - 180.0
115 PHASE = PHASE - 180.0
116 CAMPI = -CAMPI
117 PHASE = PHASE - 180.0
118 CAMPI = -CAMPI
119 WRITE(6, 221)IJ, CAMPI, PHASE, CAMP2, PHASE2
221 FORMAT(3x, 13, 3x, E16.8, 3x, E16.8, 3x, E16.8)
220 CONTINUE
WRITE(6, 393) NASSUM
393 FORMAT(3x, 24HNUMBER OF ASSUMPTIONS = , I
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1119
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                                                                                                                                                                                                                                                                                                                  22 IF (ABS (CTDPR (N-I+1)) GT .0.0) GO TO 196 PHASE2 = ATAN(DTDPR (N-I+1)/FAKE)

26 PHASE2 = ATAN(DTDPR (N-I+1)/CTDPR (N-I

27 FHASE2 = ATAN(DTDPR (N-I+1)/CTDPR (N-I

28 CAMP2 = CTDPR (N-I+1)/COS (PHASE2)

40 CAMP2 = CTDPR (N-I+1)/SIN(PHASE2)

45 PHASE2 = 57.29578 *PHASE2

46 CAMP2 = GTDPR (N-I+1)/SIN(PHASE2)

47 PHASE2 = PHASE2 - 180.0

48 CAMP2 = PHASE2 + 180.0

49 PHASE = ATAN(BTDPR (N-I+1)/FAKE)

49 PHASE = ATAN(BTDPR (N-I+1)/FAKE)

40 TO 293

41 CAMP2 = NASSUM + 1

42 CAMP2

43 CAMP2 = NASSUM + 1

44 CAMP2 = NASSUM + 1

45 CAMP2 = NASSUM + 1

46 CAMP2 = NASSUM + 1

47 CAMP2 = NASSUM + 1

48 CAMP2 = NASSUM + 1

49 CAMP2 = NASSUM + 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    GO TO 175
WAMP = WS / SIN( P
PHASE3 = 57.29578
IF (WAMP .GE . 0.0)
IF (PHASE3 = PHASE3 +
GO TO 198
PHASE3 = PHASE3 +
WAMP =-WAMP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     180.0
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10 292
30 TO
                                                                                     PHASE2 W
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397
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  29
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WRITE(6,258)
*FORMAT(1H1,73H I AMPLITUDE FEEL
NASSUM = 0.0
DD 257 I =1.N
IJ = N-I+1
FE8 = ATDPR(N-I+1) - CTDPR(N-I+1)
FE8 = ATDPR(N-I+1) - DTDPR(N-I+1)
IF(ABS(FE8) .GT. 0.0) GO TO 398
NASSUM = NASSUM + 1
IF(ABS(FE8) .GT. 0.0) GO TO 398
NASSUM = NASSUM + 1
IF(ABS(FE8) .GT. 0.0) GO TO 398
NASSUM = NASSUM + 1
IF(ABS(FEAMP2 .GE. 0.0) GO TO 345
IF(FEAMP2 = FE8 / SIN(PHASE5) .GT. 0.0
FEAMP2 = FEAMP2 .GT. 0.0 .GO TO 345
IF(ABS(FE6) .GT. 0.0) GO TO 345
PHASE5 = ATDPR(N-I+1) + CTDPR(N-I+1)
IF(ABS(FE6) .GT. 0.0) GO TO 345
PHASE4 = ATAN(FE7 / FE6)
NASSUM = NASSUM + 1
IF(ABS(FE6) .GT. 0.0) GO TO 395
PHASE4 = ATAN(FE7 / FE6)
PHASE4 = ATAN(FE7 / FE6)
FEAMP = FE6 / COS(PHASE4) .GT. 0.0
FEAMP = FE6 / COS(PHASE4) .GT. 0.0
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           PO 320 I=1, N
ETOPR(I) = ETOPI
CONTINUE
FORMAT(IH1, 33H
CALL MAP
PO 322 I=1, N
ETOPR(I) = 0.0
                                                                                         AEQ(I) = ATDPR(
BEQ(I) = BTDPR(
CONTINUE
WRITE(6;311)
CALL MAP
                                                                                                                                                         DO 300 I=1 N

AEQ(I) = ATDPR(

BEQ(I) = BTDPR(

CONTINUE

WRITE(6;310)

CALL MAP
                                                                                                                                                                                                                                         IF ( FEAMP .GE. 0.0) GO TO 255
IF ( PHASE4 .GT. 0.0) GO TO 245
IF ( PHASE4 = PHASE4 + 180.0
GO TO 248
PHASE4 = PHASE4 - 180.0
FEAMP = -FEAMP
WRITE(6,256)IJ, FEAMP, PHASE4, FEAMP2, PHASE5
FORMAT(3X,13,3X,E16.8,3X,E16.8,3X,E16.8)
CONTINUE
WRITE (6,393) NASSUM
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= ATDPR(I)
= BTDPR(I)
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= BTOPR(I)
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= ETDPR(I) +
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3-WCONST*((3/3470))
4CTDPR(N-I+1)))
4CTDPR(N-I+1))
8EQ (N-I+1) = WCONST * ((DTDF(N-I+1)-FSY(I-I+1)) -FSY(I-I+1)) -FSY(I-I+1))
2FUK*((ESY(N-I+1)*((BDY(N-I+1)-DDY(N-I+1)-DDY(N-I+1)))
302 CONTINUE
WRITE(6;312)
312 FORMAT([H1,20H OMEGA = WC + WS)
CALL MAP
                                                                                                                                                                                                          0000
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                                          S
                                                                                       DO 303 I=1N

AEQ(I) = ATDPR(I)

PEQ(I) = BTDPR(I)

CONTINUE

3 FORMAT(1H1, 20H FE

FORMAT(1H1, 20H FE

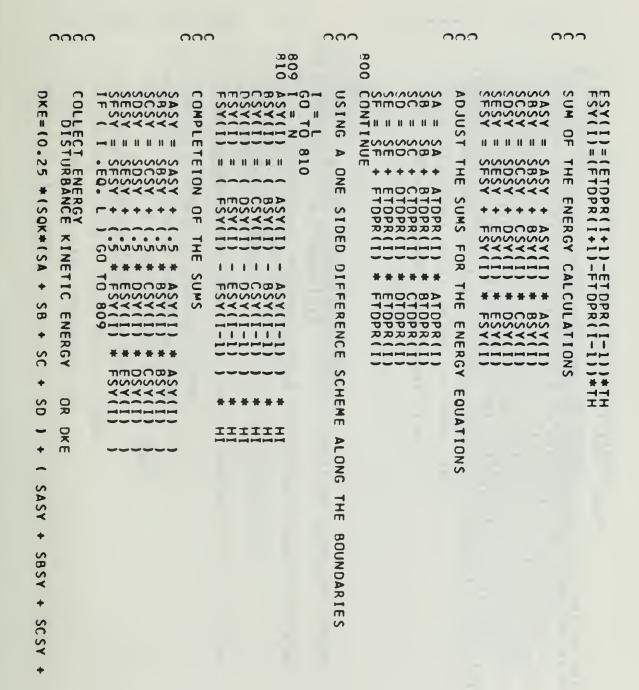
CONTINUE

WRITE(61314)

FORMAT(1H1, 20H FE

CALL MAP
                          GO TO 3
BETA = 2.29E-11
WRITE(6.5)
FORMAT(2X.36H*
GO TO 9
GO TO 9
                                                          CALL MAT
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IF (NEWMAN.LT.2)
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I-I+1) * ATDPR(N-I+1))
+1))-SQK*(BTDPA(N-I+1)
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DIMENSION ATDPA(100), BTDPA(100), CTDPA(100), DTDPA(100), ETDPA(100), *FTDPA(100), ATDPR(100), BTDPR(100), CTDPR(100), DTDPR(100), ETDPR(100), ETTPR(100), ETTPR(100), ETTPR(100), ETTPR(100), ETTPR(100), ETTPR(100), ETDPR(100), ETTPR(100), ETDPR(100), ETDPR(100), ETDPR(100), ETDPR(100), ETDPR, ETTPR, ETTPR
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20 FNED = DKE + DPE FNEM = ENMKE + ENMPE TOTE = ENED + ENEM WRITE (6 24) DKE DPE + E 24 FORMAT (140 6 H DKE = + E 2MPE = + E16 8 B) ENED ENEM 20 FORMAT (140 22H DISTRUEND + E16 8 19H TOTAL ENERGY END PIMENSIGN ATDPA(100), BTDPA(100), CTDPA(100), DTDPA(100), ETDPA(100), \*FTDPA(100), ATDPR(100), BTDPR(100), CTDPR(100), DTDPR(100), ETDPR(100), \*FTDPR(100), ATDF(100), BTDPR(100), CTDPR(100), DTDPR(100), ETDPR(100), \*FTDPR(100), ETDPR(100), ETDPR(100), \*FTDPR(100), ETDPR(100), \*FTDPR(100), \*FTDPR(100), \*FTDPR(100), \*FTDPR(100), \*FTDPR(100), \*TTPR(100), \*FTDPR(100), \*TTPR(100), DPE SUBROUTINE FUMPE MEAN FLOW POTENTIAL ENERGY OR ENMKE = ( 0.5 \* ( SESY + SFSY ) MEAN FLOW KINETIC ENERGY OR ENMKE DISTURBANCE POTENTIAL ENERGY OR ALCULATES EXACT SOLUTION FOR THE DATA FIELD =(SQMU \* 0.25 \* (SC + SD) ) / ANNN ENERGY IS = ( SQMU \* RCHMYR (XEQ, XTDPR, XTDPA, XTDF 0.5 \* SF ) / STRUBANCE STRUBANCE STRUBANCE PEL6.8,7H, DPE mmH = ,E16.8 MUNDE **DZZZ** ص اا ڪ =,E16.8 ,E16.8,20H **DUZZ** ,9H, MEAN **ENMKE** FLOW Ħ **™** 16.8,9H,

ENERGY

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                       45
                                                              RCHMYR TECHNIQUES ENDS HERE.
                                                                                                                                                                                                                                                                                                                                                                       ATDF ,BTDF ,CTDF

4AEQ,BEQ,CEQ,DEQ,EEQ,FEQ

5 ADY,BDY,CDY,DDY,EDY,FD
DO 458 I=1 N

XTDF(I) = XTDPA(I) + DVX(I)

CONTINUE

RETURN

END
                                                                                   DO 454 I = 1,M
DVX(M-I+1) = (VE(M-I+1) * DVX(M-I+2)) + VF(M-I+1)
CONTINUE
                                                                                                                                               DO 450 I=L,M

VD(I) = -2.0*HSQ*TIMAJ* XEQ(I)

VE(I) = 1.0 / ( VB - VE(I-1) )

VF(I) = ( VD(I) + VF(I-1))* VE(I)

CONTINUE
                                                                                                                              CALCULATES VALUES FOR EACH POINT.
                                                                                                                                                                                                                  CALCULATE COEFFICIENTS FOR NEXT STEP
                                                                                                                                                                                                                                                BOUNDARY CONDITIONS
                                                               NEXT WE PUT VALUES INTO THE FUTURE ARRAY
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SUBROUTINE MAD

PIHENSION ATDRA(100), BTDPA(100); CTDPA(100); DTDPA(100); ETDPA(100);

**FTDPA(100); ATDRA(100); BTDPA(100); CTDPA(100); DTDPR(100); ETDPA(100);

**FTDFA(100); ATDRA(100); BTDFA(100); CTDPA(100); DTDPA(100); ETDPA(100);

**FTDFA(100); ATDRA(100); DTDFA(100); DTDPA(100); ETDPA(100);

**FTDFA(100); ATDRA(100); DTDPA(100); DTDPA(100); ETDPA(100); DTDPA(100); DTDP
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                 4444

4444
                                                                                                                                                                                                                                                                                                                                                                                                                             ASY(I)=(ATDPR(I+1)-ATDPR(I-1))*TH

BSY(I)=(BTDPR(I+1)-BTDPR(I-1))*TH

CSY(I)=(CTDPR(I+1)-CTDPR(I-1))*TH

DSY(I)=(DTDPR(I+1)-CTDPR(I-1))*TH

ESY(I)=(ETDPR(I+1)-ETDPR(I-1))*TH

FSY(I)=(FTDPR(I+1)-FTDPR(I-1))*TH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 120 I=L,M
GLOB(I) = { ADY(I)-CDY(I) } -SQK * ( ATDPA(I) - CTDPA(I)
GLOB( I+N) = (BDY(I)-DDY(I) ) - SQK*(BTDPA(I)-DTDPA(I) )
CONTINUE
DO 500 I=L,M
                                                                                                                                                                                                                                                                                                                BUDD
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                                                                                                                                                                                                                                                                                                                                  FLE
) = (ATDPR(I+1) + ATDPR(I-1) - 2.0 *
) = (BTDPR(I+1) + BTDPR(I-1) - 2.0 *
) = (CTDPR(I+1) + CTDPR(I-1) - 2.0 * CTDPR(I-1) + CTDPR(I-1) - 2.0 + CTDPR(I-1) + CTDPR(I
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FOR CEO AND DEO, VB DOES NOT CHANGE

CALL CALL

2.0 + HSQ \* SQK
RCHMYR (AEQ, ATDPR, ATDPA, ATDF)
RCHMYR(BEQ, BTDPR, BTDPA, BTDF)

VB =

2.0 + HSQ\*PKMU RCHMYR (CEQ,CTDPR,CTDPA,CTDF) RCHMYR (DEQ,DTDPR,DTDPA,DTDF)

FOR

EEO,

**VB** 

VB = 2.0 FOR FEO, VB IS VB = 2.0 + HSQ\*SOMIJ RETURN END

CEQ(I) = FUK\*((SQK+CONC)) + (FSY(I)\*BTDPR(I)\*SQM-CEQ(I) = FUK\*((SQK+CONC)) + (FSY(I)\*BDY(I)) - (ETY(I)\*CONC) = FUK\*((SQK\*FSY(I)\*CONC)) + (FTY(I)\*CONC) + (FTY(I)\*CONC) = TFUK\*((ATDPF')) + (FTY(I)\*CONC) + (FT 510 1 + (CTOPR(I)\*DOY FEQ(I) = TFUK\*( 1 (CDY(I)-CTOPR(I) 2 - (DTOPR(I)\*(ADY CONTINUE CALL FOR AEO AND BEQ, VB DOES NOT CHANGE HIME DERIVATIVE STEP FOR A, B, C, D, E, F THE RICHTMYER SOLUTION SY(I)\*ATDPR(I)
TY(I)\*ATDPR(I)
BETAK\*ATDPR(I) TDPR(I) + SQK (I)\*BTOPR(I))) +(ESY(I)\*DDY(I (I)\*DTOPR(I))) /(I)#ATDPR(I) /(I)#ATDPR(I ( BTOPR(I) + ADY(I))
((I))
(DPR(I) + PKMU)) - (BTOPR(I) + SQK) ) - (ESY(I) \*DTOPR(I) \*PKMU)
I))-(FTY(I) \*BTOPR(I)
) - BETAK\*DTOPR(I) (ESY(I) \*PKMU\*CTDPR(I))
- (SQMU\*FSY(I) \*ATDPR(I))
) + BETAK\*CTDPR(I) - (FSY(I)\*CTOPR(I)))

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A simple two-level numerical mo				
equations is developed. Equat:				
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are used and these are known to			•	
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KEY WORDS	ROLE	wт	ROLE	wT	ROLE
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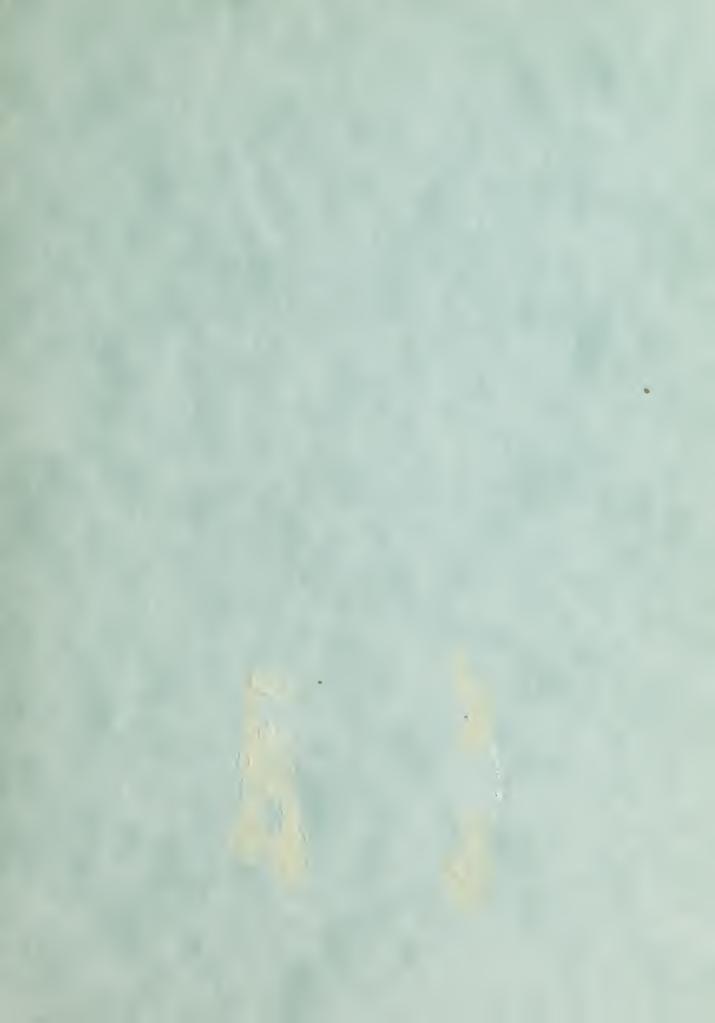
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